# Problem 6 Beach Umbrellas

## Input File: beachin.txt Output File: beachout.txt

#### Time and Memory Limits: 1 second, 1 GB

You are planning a surprise virtual beach birthday party for your best friend! As demand is high and spots are limited, you will need to book your spots on the virtual beach in advance.

The beach is divided into N segments, numbered from 1 to N from left to right. There are U umbrellas of varying sizes already placed on the beach. The ith umbrella covers all the segments from segment  $A_i$  to segment  $B_i$ , inclusive  $(A_i \leq B_i)$ .

You would like to book a continuous block of segments so that you and all your friends can hang out together. The larger the block, the better! However, you must ensure that every segment that you book is covered by at least one umbrella.

Fortunately for you, the generous caretakers of the virtual beach have given you  $\mathbf{K}$  extra umbrellas. These extra umbrellas are able to cover up to  $\mathbf{X}$  segments each. You are free to place them wherever you like (or not at all).

If you place your umbrellas optimally, what is the maximum number of segments you can book?

#### Input

- The first line of input contains the four integers N, U, K and X.
- Then U lines follow. The ith line contains the two integers  $A_i$  and  $B_i$ , indicating the ith umbrella covers all the segments from segment  $A_i$  to segment  $B_i$ .

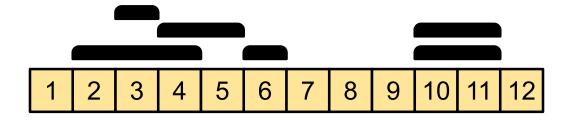
#### Output

Your program should output a single line containing a single integer: the maximum number of segments you can book.

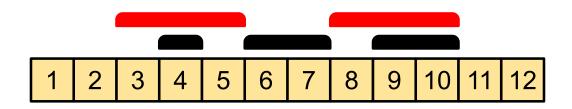
Sample Input 1	Sample Input 2	Sample Input 3
12 6 0 5	12 3 2 3	7 2 5 2
4 5	6 7	4 5
2 4	4 4	56
10 11	9 10	
3 3		
6 6		
10 11		
Sample Output 1	Sample Output 2	Sample Output 3
5	8	7

#### Explanation

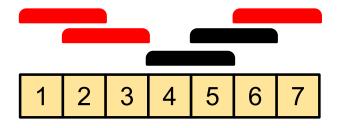
In the first sample input, there are N = 12 segments and U = 6 umbrellas. You have no spare umbrellas to place (K = 0). The largest block of segments that are all covered by umbrellas is the block from the 2nd to the 6th segment. This block contains 5 segments, which is the largest possible.



In the second sample input, there are N = 12 segments and U = 3 umbrellas. You have K = 2 spare umbrellas to place, each able to cover X = 3 segments. If you place your umbrellas as indicated in red in the diagram below, you can book the block of segments from the 3rd segment to the 10th segment. This block contains 8 segments, which is the largest possible.



In the third sample input, there are N = 7 segments and U = 2 umbrellas. You have K = 5 spare umbrellas to place, each able to cover X = 2 segments. If you place three of your spare umbrellas as indicated in red in the diagram below, you can book the block of segments from the 1st segment to the 7th segment. This block contains 7 segments, which is the largest possible. Note that the remaining two spare umbrellas are left unused.



### Subtasks & Constraints

For all test cases:

- $2 \leq N \leq 1\,000\,000\,000$ .
- $1 \leq U \leq 100\,000.$
- $\bullet \ 0 \leq K \leq 1\,000\,000\,000.$
- $1 \leq X \leq N$ .
- $\bullet \ 1 \leq A_i \leq B_i \leq N, \, {\rm for \ all \ } i.$

Additionally:

- For Subtask 1 (7 marks),  $\mathbf{K} = \mathbf{0}$  and  $\mathbf{N} \leq 100\,000$ .
- For Subtask 2 (18 marks),  $\mathbf{X} = \mathbf{1}$  and  $\mathbf{N} \leq \mathbf{100000}$ .
- For Subtask 3 (23 marks),  $\mathbf{K} = \mathbf{1}$  and  $\mathbf{N} \leq \mathbf{100000}$ .
- For Subtask 4 (40 marks),  $\mathbf{K} \leq \mathbf{5}$  and  $\mathbf{N} \leq \mathbf{100\,000}.$
- For Subtask 5 (12 marks), there are no special constraints.

There are no hints available for this problem.